

Sensor Placement Optimization for Expansion of Mixed-Domain Dynamic Response





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Motivation

Methods & Results

- Experimental Setup
- Finite Element Model
- Neuromorphic Data Collection
- Mixed Domain Expansion

• Conclusions & Future Work

Vibration response data is desired to characterize structural responses.



[Honeywell Aerospace]

Vibration Environments

Shock Environments



4 Spatial resolution can be limited by the use of physical sensors such as accelerometers.



Channel Count Limits

Mass Loading Effects

Full-field measurements can be achieved using a variety of technologies.



[Polytec]

Laser Doppler Vibrometer (LDV)

Digital Image Correlation (DIC)

[M. Mylo and S. Poppinga, 2024]



Neuromorphic imaging is an emerging technique in acquiring full-field vibration measurements.



[H.Kimm, 2016]

Events are triggered when changes in brightness exceed a set threshold per pixel, at a given location and time.

```
Event stream e = (x, y, p, t) p = Polarity: brightness change (+1,-1)
t = time of event
```

Benefits: less expensive (the camera cost and less data to process), low-latency

A low-latency alternative to full-field data acquisition is to expand vibration responses from accelerometer data at limited measurement points.

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Neuromorphic imaging and expansion procedures are both low-latency techniques to achieve full-field response information with different requirements.



- Relies on pre-test analysis to select optimal DOF sets
- Requires a FEM to generate mode shapes

• Varying levels of fidelity and confidence in the results

[iniVation]

• High displacement = more coherent data

Neuromorphic imaging and expansion procedures are both low-latency techniques to achieve full-field response information with different requirements.



Could combining neuromorphic imaging and model-based expansion lead to improved low-latency estimation of full-field responses? The goal of this research was to investigate how to integrate neuromorphic imaging data with responses from accelerometers in a single expansion procedure.

- 1) Exploring DOF selection methods to combine accelerometer and neuromorphic imaging data locations
- 2) Implementing the resulting mixed-domain expansion (acceleration + displacement)

Broader Impacts

Big Picture

Contribute to active areas of research

Develop a foundation for an improved approach to acquire low-latency full-field response data



Develop methods to provide real-time response information for vibration control

Mixed domain expansion was achieved through the following steps.

Conduct Modal Tests

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Refine the Finite Element Model

Collect and Process Neuromorphic Imaging Data

Conduct DOF Selection

Compute and Compare Single and Mixed Domain Expansion

¹² This investigation was performed using a wing-shaped aluminum plate bolted to an aluminum block.



Experimental Test Setup

Neuromorphic Camera



[iniVation]

Impact Hammer soft plastic tip (10mV/lbf sensitivity)





24 Uniaxial Accelerometers (10mV/g sensitivity)



[PCB Piezotronics]

29 Node mesh 24 DOFs

Foam Poster Board

[PCB Piezotronics]

A finite element model was refined to represent the experimental setup.



Added point masses for accelerometers

Free-Free Boundary Conditions

Hexahedral Mesh About 770,000 elements A Modal Assurance Criteria (MAC) was created to compare the experimental mode shapes with the model mode shapes.



| Natural Frequencies (Hz) | | | |
|--------------------------|-------|--------------|---------|
| Mode # | Model | Experimental | % Error |
| 1 | 25.5 | 20.8 | 22.5% |
| 2 | 59.2 | 55.7 | 6.3% |
| 3 | 89.0 | 83.9 | 6.1% |
| 4 | 167.8 | 162.2 | 3.5% |
| 5 | 223.9 | 217.2 | 2.7% |
| 6 | 288.9 | 283.1 | 2.0% |
| 7 | 341.4 | 338.4 | 0.9% |
| 8 | 406.7 | 397.3 | 2.4% |
| 9 | 496.3 | 488.7 | 1.6% |
| 10 | 549.8 | 542.5 | 1.3% |

¹⁶ This model is acceptable for the expansion due to the highly correlated mode shapes.

Model Mode 1

Experimental Mode 1



x y z

Neuromorphic imaging data was collected using a DVXplorer mini camera.



DVXplorer Mini

Spatial Resolution: 640 x 480 pixels

Event rate: 450 million events per second throughput



CSV File

The neuromorphic camera was calibrated by first finding the pixel to mm conversion factor.



Displacement was calculated using the conversion factor, and the results were fine tuned using LDV data





20 Neuromorphic imaging data was collected from three nodes for this experiment.

Camera on Tripod

1 inch distance

• Measured Node: 1, 5, 7

Timpact Node: 3





Displacement data was refined using the previous postprocessing methods.



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Acceleration response data was computed in the time and frequency domain.



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Bandwidth of interest: 10 to 200Hz

Two DOF selection methods were explored to pick the best DOF set to use in the expansion.

Effective Independence

[D.C. Kammer, 1991]

Uses a computation of the fractional contribution of each sensor location to the linear independence of the mode shapes

 $\mathbf{E} = \mathbf{U}_{\mathbf{a}} \left[\mathbf{U}_{\mathbf{a}}^{T} \mathbf{U}_{\mathbf{a}} \right]^{-1} \mathbf{U}_{\mathbf{a}}^{T}$

 U_a is the matrix of mode shapes U partitioned to the reduced set of a DOF.

The minimum values of E_{diagonal} are found and the associated DOF are removed from the candidate set.

Condition Number Optimization

[B.C. Owens et al, 2020]

- 1. Each DOF is removed one at a time
- 2. The condition number of the remaining set is computed
- 3. The set with the best (lowest) condition number is selected
- 4. Process repeated until desired number of DOF is reached

Fifteen DOFs were selected to use 10 modes within the expansion.





Effective Independence



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Selected DOFs

Removed DOFs

System Equivalent Reduction Expansion Process (SEREP) was the modal expansion method utilized.



Where:

- Φ_{new} is mode shape matrix of all DOFs from the model (24 DOFs x 10 Modes)
- $\Phi^+_{measured}$ is mode shape matrix of the selected DOF set from the model (15 DOFs x 10 Modes)
- *x_{measured}* is experimental acceleration response data of the selected DOFs (15 DOF x n frequency steps)
- *x_{new}* is estimated acceleration response data of all DOFs (24 DOF x n frequency steps)

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[J. O'Callahan et al, 1989]

Mixed Domain Expansion was achieved by incorporating neuromorphic acceleration data into $x_{measured}$.



Mixed domain expansion estimates to the block represent the measured response data relatively well.



Mixed domain expansion estimates to the wing are more noisy than estimates to the block





Single Domain

Mixed Domain

RMSE: 0.13

RMSE: 0.10

Manual Selection Method

³⁰ Three key conclusions can be drawn from this work.

Mixed domain expansion with neuromorphic data and accelerometers **can** be done



Developed a **foundation** for this mixed domain expansion process

- Collected displacement from a neuromorphic camera
- Explored two DOF selection methods
- Converted displacement to acceleration to compute a mixed domain SEREP expansion

Expanding to the **smaller displacements** of the block has **less noisy** estimates than the higher displacement point of the wing



Four areas could be further improved in future work.

Refine the model

- Better replicate boundary conditions
- Increase number of nodes to expand to



Explore DOF selection methods

- Sensor Elimination using Auto-Modal Assurance Criterion (SEAMAC)
- Modal Projection Error (MPE)



Improve neuromorphic camera data

- Refine calibration methods
- Improve post processing methods



DVXplorer Mini

Test on a different structure

- More flexible structure with higher displacement
- More modes at lower frequencies



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